



Determination of 50% endpoint titer using a simple formula

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Abstract

Two commonly used methods for calculating 50% endpoint
using serial dilutions are Spearman-Kärber method and
Reed and Muench method. To understand/apply the
above formulas, moderate statistical/mathematical skills
are necessary. In this paper, a simple formula/method for
calculating 50% endpoints has been proposed. The formula
yields essentially similar results as those of the Spearman-
Kärber method. The formula has been rigorously evaluated
with several samples.

Key words: Endpoint dilution; TCID₅₀; Spearman-Kärber;
Reed and Muench

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Core tip: The formula described in this manuscript can be
used to calculate 50% endpoint titre such as TCID₅₀%,
LD₅₀, TD₅₀, etc., in addition to the currently existing
methods. The proposed formula can be applied without
the help of calculator or computer.

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TO THE EDITOR

Currently, there are two methods (formulas) viz., Reed
and Muench^[1] and Spearman-Kärber^[2,3] are commonly
employed for the calculation of 50% endpoint by serial
dilution. To understand/apply these methods, moderate
mathematical skills along with calculator or computer
are essential. Here, I have proposed a simple formula
to calculate the 50% endpoint titre and this formula can
be used in addition to Reed and Muench or Spearman-
Kärber, methods but not exclusively at this point. In
the following section, the newly proposed method is
compared with two commonly used methods viz., Reed
and Muench and Spearman-Kärber.

Reed and Muench method

\log_{10} 50% end point dilution = \log_{10} of dilution showing
a mortality next above 50% - (difference of logarithms
 \times logarithm of dilution factor).

Generally, the following formula is used to calculate
"difference of logarithms" (difference of logarithms is
also known as "proportionate distance" or "interpolated

Table 1 Calculation of virus titre in mice using the Reed and Muench method

Log ₁₀ virus dilution	Mice		Cumulative total			Percent mortality
	Died	Survived	Died	Survived	Total	
-1	10	0	57	0	57	57/57 × 100 = 100
-2	10	0	47	0	47	47/47 × 100 = 100
-3	10	0	37	0	37	37/37 × 100 = 100
-4	10	0	27	0	27	27/27 × 100 = 100
-5	10	0	17	0	17	17/17 × 100 = 100
-6	6	4	7	4	11	7/11 × 100 = 63
-7	1	9	1	13	14	1/14 × 100 = 7

Difference of logarithms = (63-50)/(63-7) = 0.23; log₁₀ 50% end point dilution = -6 - (0.23 × 1) = -6.23; 50% end point dilution = 10^{-6.23}; the titre of the virus = 10^{6.23} LD₅₀/mL.

Table 2 Calculation of virus titre in mice using the Spearman-Kärber method

Log ₁₀ virus dilution	Mice	
	Died	Inoculated
-1	10	10
-2	10	10
-3	10	10
-4	10	10
-5	10	10
-6	6	10
-7	1	10

x₀ = 5; d = 1; log₁₀ of 50% endpoint dilution = - [5 - ½ + 1 (17/10)] = -6.2; 50% end point dilution = 10^{-6.2}; the titre of the virus = 10^{6.2} LD₅₀/mL.

value"): Difference of logarithms = [(mortality at dilution next above 50%)-50%]/[(mortality next above 50%)-(mortality next below 50%)].

Spearman-Kärber method

log₁₀ 50% end point dilution = - (x₀ - d/2 + d Σ n_i/n_i)
 x₀ = log₁₀ of the reciprocal of the highest dilution (lowest concentration) at which all animals are positive;
 d = log₁₀ of the dilution factor;
 n_i = number of animals used in each individual dilution (after discounting accidental deaths);
 n = number of positive animals (out of n_i).
 Summation is started at dilution x₀.

Newly proposed method

Formula 1:

log₁₀ 50% end point dilution = -[(total number of animals died/number of animals inoculated per dilution) + 0.5] × log dilution factor.

Formula 2 (if any accidental death occurred):

log₁₀ 50% end point dilution = -(total death score + 0.5) × log dilution factor.

Table 3 Calculation of virus titre in mice using the new method

Log ₁₀ virus dilution	Mice		Death score
	Died	Inoculated	
-1	10	10	10/10 = 1
-2	10	10	10/10 = 1
-3	10	10	10/10 = 1
-4	10	10	10/10 = 1
-5	10	10	10/10 = 1
-6	6	10	6/10 = 0.6
-7	1	10	1/10 = 0.1
Total	57		5.7

By using formula 1: log₁₀ 50% end point dilution = - (57/10 + 0.5) × 1 = -6.2; 50% end point dilution = 10^{-6.2}; the titre of the virus = 10^{6.2} LD₅₀/mL.
 By using formula 2: log₁₀ 50% end point dilution = - (5.7 + 0.5) × 1 = -6.2; 50% end point dilution = 10^{-6.2}.

Comparison of the newly proposed and existing methods with an example of virus titration in mice: For simplicity, it is assumed that 1 mL of each dilution was inoculated (Tables 1-3).

The newly proposed formula has been intensively validated with several samples and essentially yields the same results as those by the Spearman-Kärber method. Therefore, the newly proposed method can be used in addition to the existing methods but not exclusively at this point.

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