



## Determination of 50% endpoint titer using a simple formula

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the assay and wrote the letter.

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### Abstract

Two commonly used methods for calculating 50% endpoint  
using serial dilutions are Spearman-Kärber method and  
Reed and Muench method. To understand/apply the  
above formulas, moderate statistical/mathematical skills  
are necessary. In this paper, a simple formula/method for  
calculating 50% endpoints has been proposed. The formula  
yields essentially similar results as those of the Spearman-  
Kärber method. The formula has been rigorously evaluated  
with several samples.

**Key words:** Endpoint dilution; TCID<sub>50</sub>; Spearman-Kärber;  
Reed and Muench

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**Core tip:** The formula described in this manuscript can be  
used to calculate 50% endpoint titre such as TCID<sub>50</sub>,  
LD<sub>50</sub>, TD<sub>50</sub>, etc., in addition to the currently existing  
methods. The proposed formula can be applied without  
the help of calculator or computer.

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### TO THE EDITOR

Currently, there are two methods (formulas) viz., Reed  
and Muench<sup>[1]</sup> and Spearman-Kärber<sup>[2,3]</sup> are commonly  
employed for the calculation of 50% endpoint by serial  
dilution. To understand/apply these methods, moderate  
mathematical skills along with calculator or computer  
are essential. Here, I have proposed a simple formula  
to calculate the 50% endpoint titre and this formula can  
be used in addition to Reed and Muench or Spearman-  
Kärber, methods but not exclusively at this point. In  
the following section, the newly proposed method is  
compared with two commonly used methods viz., Reed  
and Muench and Spearman-Kärber.

#### Reed and Muench method

$\log_{10}$  50% end point dilution =  $\log_{10}$  of dilution showing  
a mortality next above 50% - (difference of logarithms  
 $\times$  logarithm of dilution factor).

Generally, the following formula is used to calculate  
"difference of logarithms" (difference of logarithms is  
also known as "proportionate distance" or "interpolated

**Table 1** Calculation of virus titre in mice using the Reed and Muench method

Log <sub>10</sub> virus dilution	Mice		Cumulative total			Percent mortality
	Died	Survived	Died	Survived	Total	
-1	10	0	57	0	57	57/57 × 100 = 100
-2	10	0	47	0	47	47/47 × 100 = 100
-3	10	0	37	0	37	37/37 × 100 = 100
-4	10	0	27	0	27	27/27 × 100 = 100
-5	10	0	17	0	17	17/17 × 100 = 100
-6	6	4	7	4	11	7/11 × 100 = 63
-7	1	9	1	13	14	1/14 × 100 = 7

Difference of logarithms = (63-50)/(63-7) = 0.23; log<sub>10</sub> 50% end point dilution = -6 - (0.23 × 1) = -6.23; 50% end point dilution = 10<sup>-6.23</sup>; the titre of the virus = 10<sup>6.23</sup> LD<sub>50</sub>/mL.

**Table 2** Calculation of virus titre in mice using the Spearman-Kärber method

Log <sub>10</sub> virus dilution	Mice	
	Died	Inoculated
-1	10	10
-2	10	10
-3	10	10
-4	10	10
-5	10	10
-6	6	10
-7	1	10

x<sub>0</sub> = 5; d = 1; log<sub>10</sub> of 50% endpoint dilution = - [5 - ½ + 1 (17/10)] = -6.2; 50% end point dilution = 10<sup>-6.2</sup>; the titre of the virus = 10<sup>6.2</sup> LD<sub>50</sub>/mL.

value"): Difference of logarithms = [(mortality at dilution next above 50%)-50%]/[(mortality next above 50%)-(mortality next below 50%)].

#### Spearman-Kärber method

log<sub>10</sub> 50% end point dilution = - (x<sub>0</sub> - d/2 + d Σ n<sub>i</sub>/n<sub>i</sub>)  
 x<sub>0</sub> = log<sub>10</sub> of the reciprocal of the highest dilution (lowest concentration) at which all animals are positive;  
 d = log<sub>10</sub> of the dilution factor;  
 n<sub>i</sub> = number of animals used in each individual dilution (after discounting accidental deaths);  
 n = number of positive animals (out of n<sub>i</sub>).  
 Summation is started at dilution x<sub>0</sub>.

#### Newly proposed method

##### Formula 1:

log<sub>10</sub> 50% end point dilution = -[(total number of animals died/number of animals inoculated per dilution) + 0.5] × log dilution factor.

##### Formula 2 (if any accidental death occurred):

log<sub>10</sub> 50% end point dilution = -(total death score + 0.5) × log dilution factor.

**Table 3** Calculation of virus titre in mice using the new method

Log <sub>10</sub> virus dilution	Mice		Death score
	Died	Inoculated	
-1	10	10	10/10 = 1
-2	10	10	10/10 = 1
-3	10	10	10/10 = 1
-4	10	10	10/10 = 1
-5	10	10	10/10 = 1
-6	6	10	6/10 = 0.6
-7	1	10	1/10 = 0.1
Total	57		5.7

By using formula 1: log<sub>10</sub> 50% end point dilution = - (57/10 + 0.5) × 1 = -6.2; 50% end point dilution = 10<sup>-6.2</sup>; the titre of the virus = 10<sup>6.2</sup> LD<sub>50</sub>/mL.  
 By using formula 2: log<sub>10</sub> 50% end point dilution = - (5.7 + 0.5) × 1 = -6.2; 50% end point dilution = 10<sup>-6.2</sup>.

**Comparison of the newly proposed and existing methods with an example of virus titration in mice:** For simplicity, it is assumed that 1 mL of each dilution was inoculated (Tables 1-3).

The newly proposed formula has been intensively validated with several samples and essentially yields the same results as those by the Spearman-Kärber method. Therefore, the newly proposed method can be used in addition to the existing methods but not exclusively at this point.

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